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Where is Swansea?





Swansea University





29th UK university to be established
King George V laid the foundation stone of the University in July 1920
Now over 12,500 students - 1,800 international



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Swansea University Prifysgol Abertawe

Overview

- Introduction
- > Atomistic finite element method
- Carbon nanotubes: static and dynamic analysis, buckling
- Fullerenes: vibration spectra
- Graphene: static and dynamic analysis, composites
- Nanobio sensors: vibrating nanotube and graphene based mass sensor
- > DNA mechanics
- Conclusions



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Research Areas



- Atomistic finite element method
- Nonlocal continuum mechanics for nanoscale objects
- Nanoscale bio sensors
- Uncertainty quantification in modelling and simulation
- Dynamic analysis of complex structures
- Vibration energy harvesting



Collaborators



- Prof F Scarpa (University of Bristol)
- Dr R Chowdhury, Dr C Wang, Dr A Gil, Prof P Rees (Swansea University).
- Dr T Murmu, Prof M McCarthy (University of Limerick)





Carbon Nanotubes

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Can we use continuum mechanics at the nanoslace?



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Which Young's modulus?





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Which Young's modulus?





Yakobson's paradox



Figure 1. The effective thickness *h*, Young's modulus *E*, in-plane stiffness $K = \frac{E\hbar}{1-\nu^2} \approx E\hbar$ and the bending stiffness $D = \frac{E\hbar^3}{12(1-\nu^2)}$ obtained in the literature for SWCNTs, where ν is Poisson's ratio. Among the five solid lines two represent bending stiffness $D = \frac{E\hbar^3}{12(1-\nu^2)} \approx \frac{E\hbar^3}{12} = 0.85 \text{ eV}$ and 2 eV, respectively. The other three solid lines are associated with increasing in-plane stiffness $K = \frac{E\hbar}{1-\nu^2} \approx E\hbar = 300, 360 \text{ and } 422 \text{ J m}^{-2}$. Dots 10(a–d) are given by [9]. The models and sources of the dots in the figure are listed in table 1.

Authors	Method	Wall thickness (nm)	Young's modulus (TPa)
Lu ^a	Molecular dynamics	0.34	0.974
Hernández et al.b	Tight binding molecular dynamics	0.34	1.24
Odegard et al.c	Equivalent-continuum modeling	0.69	
Li and Choud	Structural mechanics: stiffness matrix method	0.34	1.01
Jin and Yuan ^e	Molecular dynamics	0.34	1.238
Tserpes and Papanikos ^f	Structural mechanics: FE method	0.147	
Yakobson et al.g	Molecular dynamics	0.066	5.5
Zhou et al.h	Tight-binding model	0.074	5.1
Kudin et al. ⁱ	Ab inito computations	0.089	3.859
Tu and Ou-yang ^j	Local density approximation model	0.075	4.7
Vodenitcharova and Zhang ^k	Ring theory continuum mechanics	0.0617	4.88
Panatano et al.1	Continuum shell modeling	0.075	4.84
Goupalov ^m	Continuum model for long- wavelength phonons	0.087	
Wang et al. ⁿ	Ab initio calculation	0.0665	5.07

(Wang CY, Zhang LC, 2008. *Nanotechnology* **19**, 075705) (Huang Y, Wu J, Hwang K C, 2006. *Phys. Rev. B* **74**, 245413)

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Atomistic finite element method



Atomic bonds are represented by beam elements
Beam properties are obtained by energy balance

$$U_{total} = U_r + U_{\theta} + U_{\tau}$$

$$U_{axial} = \frac{1}{2} K_{axial} (\Delta L)^2 = \frac{EA}{2L} (\Delta L)^2$$

$$U_r = \frac{1}{2} k_r (\Delta r)^2 \quad U_{\theta} = \frac{1}{2} k_{\theta} (\Delta \theta)^2 \quad U_{\tau} = \frac{1}{2} k_{\tau} (\Delta \phi)^2$$

$$U_{torsion} = \frac{1}{2} K_{torsion} (\Delta \beta)^2 = \frac{GJ}{2L} (\Delta \beta)$$

$$U_{bending} = \frac{1}{2} K_{bending} (2\alpha)^2 = \frac{EI}{2L} \frac{4 + \Phi}{1 + \Phi} (2\alpha)^2$$

Scarpa, F. and Adhikari, S., "A mechanical equivalence for the Poisson's ratio and thickness of C-C bonds in single wall carbon nanotubes", Journal of Physics D: Applied Physics, 41 (2008) 085306

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Atomistic finite element method



◆ All parameters of the beam can be obtained in closed-form:



Scarpa, F. and Adhikari, S., "A mechanical equivalence for the Poisson's ratio and thickness of C-C bonds in single wall carbon nanotubes", Journal of Physics D: Applied Physics, 41 (2008) 085306



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Atomistic Structural Mechanics



For space frames:



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Atomistic FE – bending deformation of SWCNTs

Table 2. Bending modulus, thickness and Poisson's ratio for zigzag and armchair SWCNTs. Aspect ratio (tube length/tube diameter) is 20.

Radius		d	Ε	G	Y_f	
(nm)	ν	(nm)	(TPa)	(TPa)	(TPa)	ε_f
Zigzag						
0.378	0.0344	0.112	16.79	2.54	0.88	3.51×10^{-5}
0.777	0.0344	0.0853	16.77	7.61	1.078	1.84×10^{-5}
0.935	0.0344	0.0842	16.65	8.02	1.079	1.56×10^{-5}
1.1708	0.0344	0.0837	16.81	8.17	1.083	1.24×10^{-5}
Armcha	ir					
0.246	0.0344	0.0773	19.7	11.25	2.7	2.51×10^{-5}
0.585	0.0344	0.0911	14.22	5.85	1.26	1.935×10^{-5}
0.883	0.0344	0.0841	16.65	8.02	1.15	1.54×10^{-5}
1.312	0.0344	0.0836	16.89	8.25	1.075	1.12×10^{-5}

(F Scarpa and S Adhikari, 2008. J. Phys. D: App. Phys., 41, 085306)

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Atomistic FE – bending deformation of SWCNTs bundles

Similarity between hexagonal SWCNT packing bundle and structural idealization for wing boxes

Polar moment of inertia for each CNT:

$$I_c = \frac{\pi}{4} \left[\left(R + \frac{d}{2} \right)^4 - \left(R - \frac{d}{2} \right)^4 \right]$$
(1)

Polar moment of inertia for hexagonal packing:

(3)

$$I_{hex} = 4 \left(I_c + \left(3 \frac{l_0^2}{2} \right)^2 A_c \right) + 3I_c \qquad (2)$$

Flexural modulus of the nanbundle:



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 $\overline{Y}_f = Y \frac{I_{hex}}{I_h}$



Atomistic FE – bending deformation of SWCNTs bundles







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 We are interested in the changes in the mechanical properties





Carbon nanotubes with defects



(a) Ratio between mean of axial Young's modulus and pristine stiffness and (b) between standard deviation of the Young's modulus against pristine Young's modulus for armchair (n,n). Pristine Young's modulus Y_0 : 2.9, 1.36, 0.91, 0.67 TPa for a thickness d = 0.084 nm. • = 2 % NRV; • = 1.5 % NRV; • = 1 % NRV; • = 0.5 % NRV



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Fullerene

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Vibration spectra of fullerene family





Thin shell theory

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The natural frequencies of spherical fullerenes can be given by

$$\omega_{n1,2}^{2} = \frac{E}{R^{2}\rho} \Omega_{n1,2}^{2} \qquad \Omega_{n1,2}^{2} = \frac{1}{2(1-\mu^{2})} \{n(n+1) + 1 + 3\mu \pm \sqrt{[n(n+1)+1+3\mu]^{2} - 4(1-\mu^{2})[n(n+1)-2]} \}$$









Graphene

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Atomistic FE – in-plane SLGS





		-			
Author	Y_1 (TPa nm)	Y_2 (TPa nm)	v_{12}	v_{21}	d (Å)
Tu and Ou-Yang [45]	0.3	348	0.	34	0.74
Zhou et al [46]	0.3	377	0.	24	0.74
Yakobson et al [47]	0.3	363	0.	19	0.66
Caillerie et al [25]	0.2	277	0.	26	N/A
Brenner et al [15]	0.2	235	0.	41	0.62
Huang et al [17]	0.2	243	0.3	397	0.57
Kudin et al [13]	0.3	345	0.1	149	0.84
Chang and Gao [50]	0.3	360	0.	16	3.4
Cho et al [48]	0.3	386	0.1	195	3.35
Sakhaee-Pour [34]	0.337	-0.354	1.129	-1.441	3.4
Hemmasizadeh et al [24]	0.1	124	0.	19	1.317
Blakslee et al [58]	0.3	342	0.	16	3.35
Lee et al [60]	0.3	335	N	/A	3.35
Reddy et al [23]	0.228	0.277	0.43	0.52	3.4
Present FE honeycomb (AMBER)	0.517	0.342	0.523	0.509	0.82-0.99
Present FE honeycomb (Morse)	0.546	0.408	0.551	0.577	0.86-0.87
Present EHM	0.2	297	0.2	211	0.84
stretching-hinging (AMBER) Present EHM	0.3	384	0.2	213	0.74
stretching-hinging (Morse) Present EHM stretching binging shees (AMPEP)	0.1	144	0.6	517	0.84
Present EHM	0.1	169	0.6	553	0.74
stretching-hinging-shear (Morse) Present EHM-all deformation mechanisms (AMBER)	0.0	064	0.8	330	0.84
Present EHM-all deformation mechanisms (Morse)	0.0	074	0.8	348	0.74

Table 5. Graphene data from literature and present work.

(F Scarpa, S Adhikari, A S Phani, 2009. *Nanotechnology* 20, 065709) College of Engineering www.swansea.ac.uk/engineering



Atomistic FE vs Continuum – SLGS



Circular SLGS (R = 9:5 nm) under central loading. Distribution of equivalent membrane stresses.

Deformation of rectangular SLGS (15.1 x 13.03 nm²) under central loading.

Scarpa, F., Adhikari, S., Gil, A. J. and Remillat, C., "The bending of single layer graphene sheets: Lattice versus continuum approach", Nanotechnology, 21[12] (2010), pp. 125702:1-9.

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Axtomistic FE vs Continuum – SLGS



Comparison of the nondimensional force vs. nondimensional out-of-plane displacement for circular and rectangular lattice and continuum SLGS.



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Analytical approach for SLGS – honeycomb structure





C-C bonds deform under stretching and hinging

 $K_h = \frac{8k_\tau}{d^2}$ Hinging constant related to thickness d

Applying averaging of stretching and hinging deformation over unit cell:

$$E_{1} = \frac{4\sqrt{3}k_{r}K_{h}}{3d(k_{r} + 3K_{h})} \qquad E_{2} = \frac{4\sqrt{3}k_{r}K_{h}}{3d(k_{r} + 3K_{h})}$$
$$v_{21} = v_{12} = \frac{1 - K_{h}/k_{r}}{1 + 3K_{h}/k_{r}} \qquad G_{12} = \frac{\sqrt{3}K_{h}k_{r}}{3d(k_{r} + K_{h})}$$

Isotropic for "infinite" graphene sheet Orthotropic for finite size graphene and considering edge effects

F Scarpa, S Adhikari, A S Phani, 2009. Nanotechnology 20, 065709

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Analytical approach for SLGS – honeycomb structure



Unit cell made by rods withstanding axial and bending deformation

$$V_{\mathbf{a-f}} = \frac{4Lk_r}{\pi d_r^2}$$

 $Y_{g-n} = \frac{16k_{\theta}}{\pi L d_b^2}$

Equivalent Young's modulus for axial members

Equivalent Young's modulus for axial members

A **Rigidity** matrix is obtained using a lattice continuum modelling of space frames \rightarrow equivalence with plane stress formulation for a plane sheet:



F Scarpa, S Adhikari, A S Phani, 2009. Nanotechnology 20, 065709

(L Kollár and I Hegedús. Analysis and design of space frames by the Continuum Method. Developments in Civil Engineering, 10. Elsevier, Amsterdam, 1985)



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Atomistic FE – Bilayer Graphene





Equivalent to structural "sandwich" beams
C-C bonds in graphene layers represented with classical equivalent beam models
"Core" represented by Lennard-Jones potential interactions:

$$F_{ij} = -12\epsilon \left[\left(\frac{r_{min}}{y} \right)^{13} - \left(\frac{r_{min}}{y} \right)^7 \right] \qquad \begin{array}{c} r_{min} = 0.383 \text{ nm} \\ \epsilon = 2.39 \text{ meV} \end{array}$$

Dimensions $[nm \times nm]$	E _f [TPa]	G _{LJ} [TPa]	Force model
7.99×0.92	0.371	0.0142	AMBER
7.99×1.35	0.379	0.0143	AMBER
7.99×2.63	0.371	0.0143	AMBER
7.99×0.92	0.531	0.0161	Morse
7.99 × 1.35	0.535	0.0161	Morse
7.99×2.63	0.520	0.0160	Morse

E_f **=0.5 TPa** (I.W. Frank, D.M. Tanenbaum, A.M. van der Zande, P.L. McEuen, J. Vac. Sci. Technol. B 25 (2007) 2558)

¹2 Scarpa, F., Adhikari, S. and Chowdhury, R., "The transverse elasticity of bilayer graphene", Physics Letters A, 374[19-20] (2010), pp. 2053-2057.

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Mechanical vibration of SLGS



Lumped mass matrix:

 $\left[\mathbf{M}\right]_{\mathbf{e}} = diag \left[\begin{array}{ccc} \frac{m_c}{3} & \frac{m_c}{3} & \frac{m_c}{3} & 0 & 0 \end{array}\right]$

Minimisation of the Hamiltonian for the ith mode:

$$H_{i} = \frac{1}{2} \left\{ \mathbf{\Phi} \right\}_{i}^{T} \left[\mathbf{M} \right] \left\{ \mathbf{\Phi} \right\}_{i} \times \omega_{i}^{2} + \frac{1}{2} \left\{ \mathbf{\Phi} \right\}_{i}^{T} \left[\mathbf{K} \right] \left\{ \mathbf{\Phi} \right\}_{i} = \omega_{i}^{2}$$

Comparison against Molecular Mechanics model based on the eigenvalue analysis of the system Hessian matrix



Scarpa, F., Chowdhury, R., Kam, K., Adhikari, S. and Ruzzene, M., "Wave propagation in graphene nanoribbons", Nanoscale Research Letters, 6 (2011), pp. 430:1-10. Chowdhury, R., Adhikari, S., Scarpa, F. and Friswell, M. I., "Transverse vibration of single layer graphene sheets", Journal of Physics D: Applied Physics, 44[20] (2011), pp. 205401:1-11.

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Mechanical vibration of SLGS







Nanobio Sensors

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Vibration based mass sensor: CNT Swansea University Prifysgol Abertawe y(x,t)y(x,t)Point mass **Distributed mass** Chowdhury, R., Adhikari, S. and Mitchell, J., "Vibrating carbon Adhikari, S. and Chowdhury, R., "The calibration of carbon nanotube based bio-sensors", Physica E: Low-dimensional Systems and Nanostructures, 42[2] (2009), pp. 104-109. nanotube based bio-nano sensors", Journal of Applied Physics, 107[12] (2010), pp. 124322:1-8 **College of Engineering** www.swansea.ac.uk/engineering



The equation of motion of free-vibration:
$$EI \frac{\partial^4 y(x,t)}{\partial x^4} + \rho A \frac{\partial^2 y(x,t)}{\partial t^2} = 0$$

The resonance frequencies:
$$f_j = \frac{\lambda_j^2}{2\pi} \sqrt{\frac{EI}{\rho A L^4}}$$
 $\cos \lambda \cosh \lambda + 1 = 0$

The Mode shapes:
$$Y_j(\xi) = (\cosh \lambda_j \xi - \cos \lambda_j \xi)$$

 $-\left(\frac{\sinh \lambda_j - \sin \lambda_j}{\cosh \lambda_j + \cos \lambda_j}\right) (\sinh \lambda_j \xi - \sin \lambda_j \xi)$

where

$$\xi = \frac{x}{L}$$

We use energy principles to obtain the frequency shift due to the added mass.





$$f_n = \frac{1}{2\pi} \sqrt{\frac{k_{eq}}{m_{eq}}} = \frac{\beta}{2\pi} \frac{c_k}{\sqrt{1 + c_m \Delta M}}$$

where

$$\beta = \sqrt{\frac{EI}{\rho A L^4}}$$

the stiffness calibration constant

$$c_k = \sqrt{\frac{I_3}{I_1}}$$

and the mass calibration constant

$$c_m = \frac{I_2}{I_1}$$

Identification of the added mass

$$f_n = \frac{f_{0_n}}{\sqrt{1 + c_m \Delta M}} \tag{22}$$

The frequency-shift can be expressed using Eq. (22) as

$$\Delta f = f_{0_n} - f_n = f_{0_n} - \frac{f_{0_n}}{\sqrt{1 + c_m \Delta M}}$$
(23)

From this we obtain

$$\frac{\Delta f}{f_{0_n}} = 1 - \frac{1}{\sqrt{1 + c_m \Delta M}} \tag{24}$$

Rearranging gives the expression

$$\Delta M = \frac{1}{c_m \left(1 - \frac{\Delta f}{f_{0_n}}\right)^2} - \frac{1}{c_m} \tag{25}$$

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Mass of a nano object can be detected from the frequency shift Δf

$$M = \frac{\rho AL}{c_m} \frac{(c_k^2 \beta^2)}{(c_k \beta - 2\pi \Delta f)^2} - \frac{\rho AL}{c_m}$$

$$I_1 = \int_0^1 Y_j^2(\xi) \mathrm{d}\xi = 1.0$$

$$I_2 = \frac{1}{\gamma} \int_{\xi=1-\gamma}^1 Y_j^2(\xi) \mathrm{d}\xi; \quad 0 \le \gamma \le 1$$

$$I_3 = \int_0^1 Y_j^{''^2}(\xi) \mathrm{d}\xi = 12.3624$$

$$c_k = \sqrt{\frac{I_3}{I_1}} = 3.5160$$
 and $c_m = \frac{I_2}{I_1}$

Adhikari, S. and Chowdhury, R., "The calibration of carbon nanotube babio-nano sensors", *Journal of Applied Physics*, **107**[12] (2010), pp. 124322:1-8

TABLE I. The stiffness (c_k) and mass (c_m) calibration constants for CNT based bio-nano sensor. The value of γ indicates the length of the mass as a fraction of the length of the CNT.

	Cantilev	ered CNT	Bridg	ed CNT
Mass size	c_k	c_m	c_k	c_m
Point mass $(\gamma \rightarrow 0)$	3.5160152	4.0	22.373285	2.522208547
$\gamma = 0.1$		3.474732666		2.486573805
$\gamma = 0.2$		3.000820053		2.383894805
$\gamma = 0.3$		2.579653837		2.226110255
$\gamma=0.4$		2.212267400		2.030797235
$\gamma=0.5$		1.898480438		1.818142650
$\gamma = 0.6$		1.636330135		1.607531183
$\gamma=0.7$		1.421839146		1.414412512
$\gamma = 0.8$		1.249156270		1.248100151

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Mass of a nano object can be detected from the frequency shift Δf





Vibration based mass sensor: Graphene

Vibrating graphene sheets can be used as sensors with different mass arrangements



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Vibration based mass sensor: Graphene

Relative added mass:

$$\mu = \frac{1}{c_n \left(1 - \frac{\Delta f}{f_0}\right)^2} - \frac{1}{c_n}$$

Table 1: The calibration constants for SLGS based bio-nano sensor due to four possible configurations of attached mass.

lass arrangement	Calibration constant c_n
lase (a): Masses are at	$2\pi/(3\pi-8)$
he cantilever tip in a	
ne	
Case (b): Masses are in	$2\pi(1-\cos(\pi\gamma/2))^2/(3\pi-8)$
line along the width	
Case (c): Masses are in	$(3\pi\eta + [\sin((\gamma + \eta)\pi) - \sin(\gamma\pi)] - 8[\sin((\gamma + \eta)\pi) - 8[\sin((\gamma + \eta)\pi)] - 8[\sin((\gamma + \eta)\pi)] - 8[\sin((\gamma + \eta)\pi) - 8[\sin((\gamma + \eta)\pi)] - 8[\sin((\gamma + \eta)\pi)] - 8[\sin((\gamma + \eta)\pi) - 8[\sin((\gamma + \eta)\pi)] - 8[\sin((\gamma + \eta)\pi)] - 8[\sin((\gamma + \eta)\pi) - 8[\sin((\gamma + \eta)\pi)] - 8[\sin((\gamma + \eta)\pi)\pi)] - 8[\sin((\gamma + \eta)\pi)] - 8[\sin((\gamma + \eta)\pi)\pi)] - 8[\sin((\gamma + \eta)\pi)] - 8[\sin((\gamma + \eta)\pi)] - 8[\sin((\gamma + \eta)\pi)\pi)] - 8[\sin((\gamma + \eta)\pi)] - 8[\sin((\gamma + \eta)\pi$
line along the length	$\eta(\pi/2) - \sin(\gamma\pi/2)])/\eta(3\pi - 8)$
lase (d): Masses are in	$(3\pi\eta\cos(\theta) + [\sin((\gamma + \eta\cos(\theta))\pi) -$
line with an arbitrary	$\sin(\gamma \pi)] - 8[\sin((\gamma + \eta \cos(\theta))\pi/2) -$
	$\sin(\alpha \pi/2)$])/ $n\cos(\theta)(2\pi-8)$

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Vibration based mass sensor: Graphene

Vibrating graphene sheets can be used as sensors with different mass arrangements





Boron Nitride Nanotube and Nanosheets

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Axial vibration of BNNT

(a) (a) Axial vibration and its associated frequency of (b) zigzag and (c) armchair BNNTs given by the MM simulations (discrete dots) and a column model with Young's modulus 1TPa (solid lines).



Chowdhury, R., Wang, C. W., Adhikari, S. and Scarpa, F., "Vibration and symmetry-breaking of boron nitride nanotubes", Nanotechnology, 21[36] (2010), pp. 365702:1-9.

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Torsional vibration of BNNT





Chowdhury, R., Wang, C. W., Adhikari, S. and Scarpa, F., "Vibration and symmetry-breaking of boron nitride nanotubes", Nanotechnology, 21[36] (2010), pp. 365702:1-9.

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Optimised shape of BNNT







(d)

Optimized configuration of armchair BNNTs: (a) (3, 3), (b) (4,4) and (c) (6,6) with the aspect ratio 15, and (d) short (6, 6) with the aspect ratio 2.

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Mechanical property of BN Sheets





 $\bar{Y} = \frac{8\sqrt{3}C_{\rho}}{18 + r_{BN}^2 \left(\frac{C_{\rho}}{C_{\rho}}\right)}$ $\bar{\nu} = \frac{r_{BN}^2 \left(\frac{C_{\rho}}{C_{\theta}}\right) - 6}{18 + r_{BN}^2 \left(\frac{C_{\rho}}{C_{\theta}}\right)}$ $\bar{G} = \frac{2\sqrt{3}C_{\rho}}{3 + 18r_{BN}^2\left(\frac{C_{\rho}}{C_{\gamma}}\right)}$

Example of armchair (4, 0) BN sheet. Boron atoms are in red, nitrogen atoms are in green.

Boldrin, L., Scarpa, F., Chowdhury, R., Adhikari, S. and Ruzzene, M., "Effective mechanical properties of hexagonal boron nitride nanosheets", Nanotechnology, 22[50] (2011), pp. 505702:1-7.

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DNA Mechanics

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From protein data bank file to ANSYS input file – a new code for automatic translation







Material properties of the beams are obtained depending on the nature of the bonds





Mode 3 (MM:33.679; FE 38.768 GHz)

Mode 6 (MM:111.696; FE 112.71 GHz)

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Conclusions



- Atomistic finite element method is developed for general nanosalce structures:
 - Carbon nanotube
 - Fullerenes
 - Graphene
 - Nanoscale bio sensors
- Programs have been written to convert pdb files to Finite Element geometry file and material properties
- Encouraging results compared to MM simulation were obtained
- Future: nonlinearity, large-scale problems such as proteins & nanocomposites, molecular dynamic simulations, experimental validation

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